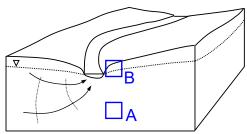
Vadose Zone Hydrology

Objectives

- 1. Review basic concepts and terminology of soil physics.
- 2. Understand the role of water-table dynamics in GW-SW interaction.

Darcy's law is useful in region A.

Some knowledge of soil physics is required to understand the processes in region B.



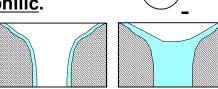
Important differences between A and B:

- Storage change is due to the compression/expansion of pore space in A. It is due to the filling/draining of pores in B.
- Hydraulic conductivity (K) is dependent on water content in B.

Water storage in unsaturated soil

Mineral surfaces have uneven distribution of + and - charges, and it loves to hold water - <u>hydrophilic</u>.

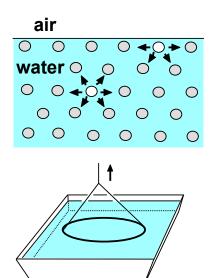
Electrostatic attraction explains the storage of a thin film of water. The rest is held in soil pores by surface tension.



Molecules near the air-water interface feel stronger force inward than outward. A body of water tends to have the minimum surface area for a given volume.

One needs to apply some force to increase the surface area of air-water interface. This force is called surface tension.

Unit of surface tension?



Capillary tube

The condition of water in soil pores is similar to water in a capillary tube (thin glass tube).



λ

 F_{g}

а

From the balance of downward force F_g (gravity) and upward force F_s (surface tension 'pull'), it can be shown that:

$$a = \frac{2\sigma}{\rho g} \frac{1}{r} \times \cos \lambda$$
 Young-Laplace equation

 ρ : density of water (1000 kg m⁻³)

 σ : surface tension (\cong 0.07 N m⁻¹ at 20 °C)

 λ : contact angle (\cong 0 for most minerals; i.e. $\cos \lambda \cong$ 1)

Example:

Estimate the height of capillary rise (*a*) in hypothetical mineral soil having a pore radius (*r*) of 0.1 mm.

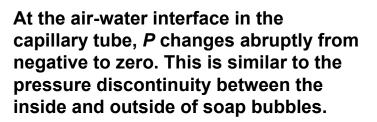
Concept of negative pressure

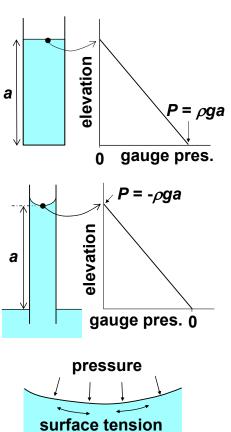
'Gauge pressure' is used in hydrology, which is referenced to atmospheric pressure: i.e. P = 0 at the water surface.

In a static water container (no capillary effects), *P* increases linearly with depth.

In a capillary tube, P also increases with depth, but P = 0 at the bottom.

P < 0 in water!





Soil matric potential

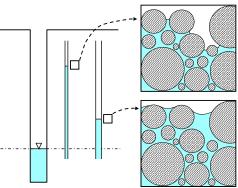
In a similar manner, P and ψ in soils above the water table is negative. The magnitude of negative pressure is called <u>soil</u> <u>tension</u>. In soil physics, ψ is called soil <u>matric potential head</u>.

Soil particles are applying tension force to keep water suspended above the water table.

Under the hydrostatic condition (i.e. no flow), ψ is equal to the height above the water table.

Recall from Darcy's law:

 $h = z + \psi$ $\rho g h = \rho g z + \rho g \psi$



The left-hand side is called <u>total potential</u> (J m⁻³) in soil physics, consisting of gravity and matric potential. In saline soil, the effects of chemical osmosis needs to be added to total potential.

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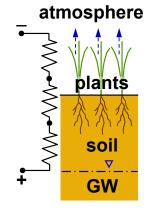
Soil matric potential represents the magnitude of energy (or work) required to remove water from soil pore spaces.

 \rightarrow Lower potential = Stronger attraction

The same matric potential is used by plant physiologists to represent the energy state of water in plant tissues.

 \rightarrow Plants 'suck' water from soil, like straws.

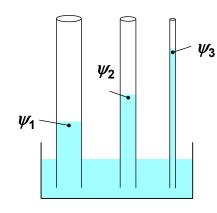
The matric potential is also related to vapour pressure in the atmosphere.



The flow of water through the <u>soil-plant-atmosphere continuum</u> is seamlessly described using ψ .

→ Basis for physically-based equations for estimating evapotranspiration (e.g., Penman-Monteith).

Soil Water Characteristics



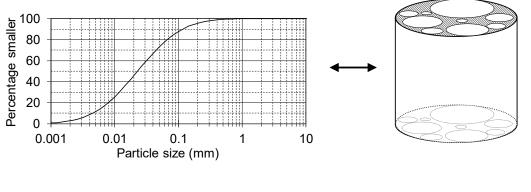
The height of capillary rise (and the magnitude of ψ) is related to the radius (*r*) of capillary tubes.

$$|\psi| \cong \frac{2\sigma}{\rho_w g} \frac{1}{r}$$

Smaller tubes have stronger ability to retain water against gravity.

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Consider a bundle of different-size capillary tubes as a simplified model of soil pores.

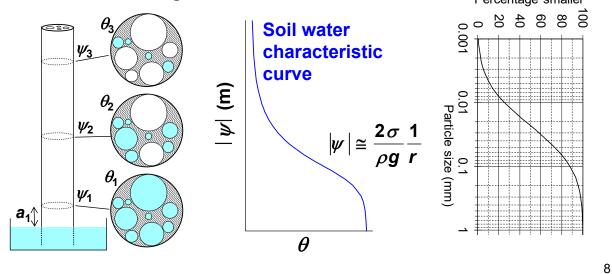


In each slice of the bundle, volumetric water content (θ) is defined by the sum of water-filled areas divided by total area.

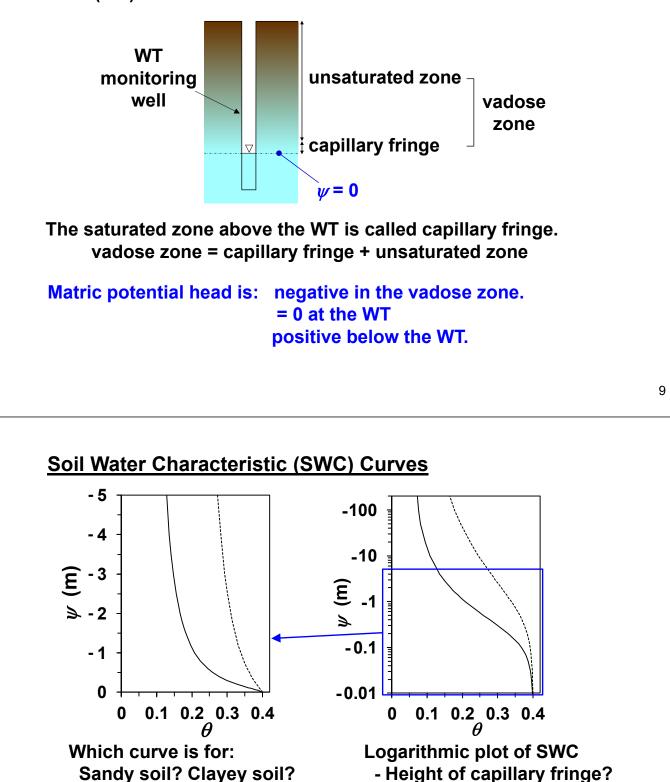
 $\theta = V_{\text{water}} / V_{\text{total}} \approx A_{\text{water}} / A_{\text{total}}$

At Level 1 ($\psi_1 = -a_1$), the bundle is saturated because all tubes are holding water.

As large tubes become empty at some height above the water table, θ decreases with height.



In real soils under the hydrostatic condition (i.e. no flow of water), θ generally decreases with the height above the water table (WT).

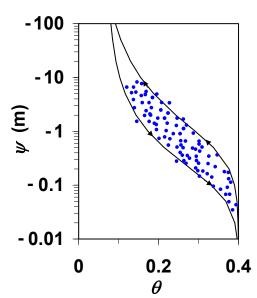


What does a very low value of ψ (e.g., -100 m) represent?

- Water is present in very small pores only.
- Easily accessible water has been taken up by evapotranspiration.

Hysteresis of SWC

The θ - ψ relations of real soil have hysteresis. Drying curves have higher θ for the same ψ than wetting curves, due to pore connectivity and complex geometry.



However, hysteresis is commonly ignored in hydrological models.

 \rightarrow See Jury and Horton (2004. Soil Physics, Ch. 2) for more detailed discussion.

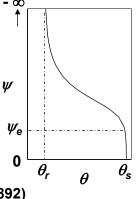
11

Soil water characteristic functions

Many empirical and theoretical equations have been proposed to represent the relation between ψ and θ .

Definitions

water saturation, $S_w = \theta / \theta_s$ effective water saturation, $S_e = (\theta - \theta_r) / (\theta_s - \theta_r)$ θ_s : saturation water content (= porosity) θ_r : residual water content ψ_s : air entry pressure head (m)



van Genuchten equation (1980. Soil Sci. Soc. Am. J., 44: 892) $S_e = 1 / [1 + (\alpha |\psi|)^n]^m$ $\alpha (m^{-1})$: reciprocal of 'capillary length' ∞ height of capillary fringe n: dimensionless constant m: dimensionless constant (commonly m = 1 - 1/n)

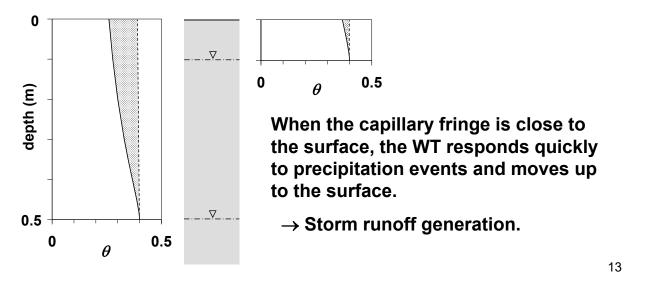
Other equations relate S_w or S_e to ψ or ψ/ψ_e in various functional forms.

Dynamic response of capillary fringe

For the sandy soil in Slide 10, suppose a hydrostatic condition with the WT 0.5 m below the surface.

A sizable amount of water is required to saturate the soil column.

For the same sandy soil, suppose that the WT is 0.1 m below the surface. Only a small amount of water addition is required to saturate the soil and bring the WT to the surface.



Unsaturated hydraulic conductivity

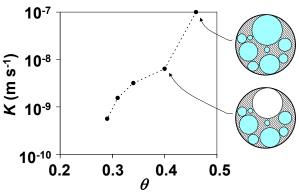
In the Darcy's law section, we saw that the hydraulic conductivity (*K*) of saturated sands is proportional to (pore diameter)².

We also saw that as the soil dries, average diameter of waterholding pores become smaller.

What does this mean?

The graph shows *K* as a function of θ for clay-rich soils in the Canadian prairies. Hayashi et al. (1997. *Soil Sci.*, 162: 566)

 $K(\theta)$ is highest at saturation and decreases with θ .



Effects of macropores

SW-GW interaction occurs mainly in shallow subsurface environments, where macropores (root holes, animal burrows, fractures, etc.) may provide the main conduits for water. $K(\theta)$ drops rapidly as the macropores drain.

Example:

Consider a root hole with a diameter of 2 mm. Is there water in this hole, if it is at 5 cm above the WT?

Richards equation

In the vadose zone: 1) Darcy's law needs to account for $K(\theta)$ function, and 2) storage is due to the change in θ . Therefore, the flow equation takes the form of:

$$\frac{\partial}{\partial x} \left(K_x(\theta) \frac{\partial h}{\partial x} \right) + \frac{\partial}{\partial z} \left(K_z(\theta) \frac{\partial h}{\partial z} \right) = \frac{\partial \theta}{\partial t} \qquad \text{Eq. [1]}$$

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The Richards equation plays the fundamental role in the analysis of SW-GW interaction involving the WT dynamics.

By solving the Richards equation, we try to determine θ at any time and space. However, *K* is dependent on θ , so we cannot solve the equation without knowing the solution first! This type of equation is called <u>non-linear</u>.

Non-linear equations are very difficult (or impossible) to solve by hand, and numerical solution on computers takes a very long time.

Therefore, simplified approach to obtain approximate answers is preferred in the studies of SW-GW interaction.

Dupuit-Forchheimer (D-F) approximation

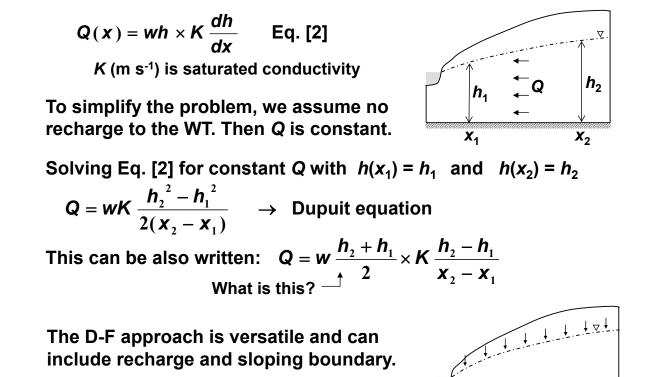
Suppose a vertical cross section with a stream. Actual flow field is two-dimensional involving the vadose zone.

D-F approximation assumes:

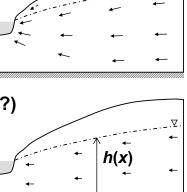
- (1) Flow in the vadose zone is very small (why?)
- (2) Flow is strictly horizontal.
- (3) Hydraulic head (*h*) is a function of *x* only, meaning *h* does not change with depth.
- (4) Aguifer has an impermeable bottom.
- (5) Steady state (no change in the WT).

Remember that h = z at the WT, so we can use the elevation of the WT as *h*. If we use the bottom of the aquifer as elevation datum. then *h* is numerically equal to saturated aguifer thickness.

Suppose that the section has a width (y-direction) of w (m). Then the flow rate Q (m³ s⁻¹) towards the stream is:



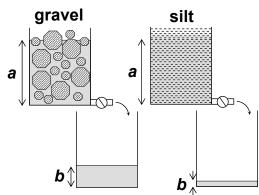
See Dingman (2002. Physical Hydrology, p. 357) Brutsaert (2005. Hydrology, p. 388)



 $\mathbf{x} = \mathbf{0}$

Specific yield and drainable porosity

When the water table (WT) is lowered in a sediment column, a significant amount of water may be retained in the sediment.



The amount of water drained per unit drop of WT is called <u>specific</u> <u>yield</u> (S_v) or drainable porosity.

For gravel,
$$S_y = b / a \cong n_p$$

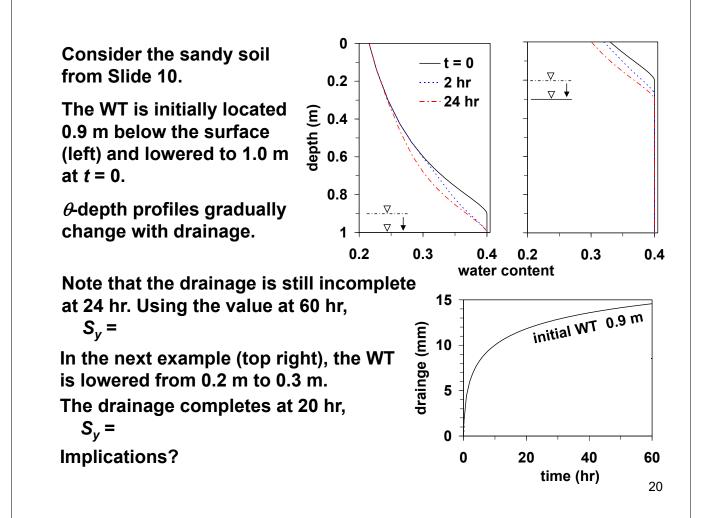
silt, $S_y = b / a << n_p$
where n_p = total porosity

Above definition of S_v or drainable porosity assumes that:

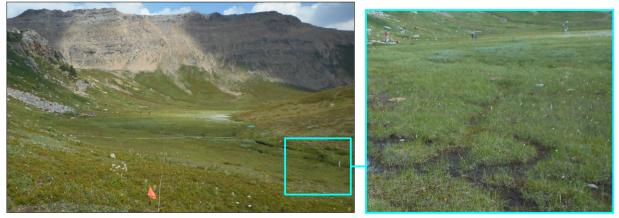
- (1) Draining or filling of pores is instantaneous
- (2) Ratio *b*/*a* is independent of the depth to the WT
- (3) Ratio *b*/*a* is independent of the size of WT drop (= *a*)

Are these assumptions valid?

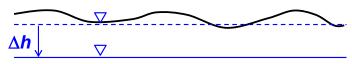
We answer this question using a numerical simulation of drainage.



Water balance of wetlands



Helen Creek watershed, Canada



Volume change = Area × $S_y \times \Delta h$

How do we define S_y ? Is it constant? See Sumner (2007. *Wetlands*, 27: 693-701)